

## CHAPTER 1 Introduction

- 1) What is the difference between a total life approach and a defect-tolerant approach?
- 2) What is HCF and LCF and what characterizes them?
- 3) What is the difference between dimensioning Safe-life or Fail-safe?
- 4) What is RFC?
- 5) What is "Leak-before-break"?
- 6) What is the influence from hydrostatic pressure on plasticity in metals?
- 7) Consider a beam, clamped in one end and of length  $L$  and bending stiffness  $EI$ . The material is ideally elastic-plastic. Determine maximum load  $P_{el}$  that can be applied at its free end without causing plasticity. At what load  $P_{max}$  is the beam fully plastic?
- 8) What are the flow surfaces according to von Mises and Tresca?
- 9) Consider a thin walled pressure vessel of length  $L$ , radius  $R$  and wall thickness  $t$ . The vessel is subjected to an inner pressure  $p$ , a torque  $M_v$  and an axial force  $P$ . Determine the effective stress.
- 10) If the flow surface is given by the function  $f(\sigma_{ij})$ , what are the implications  $f(\sigma_{ij}) > 0$ ,  $f(\sigma_{ij}) = 0$  and  $f(\sigma_{ij}) < 0$ ?
- 11) What is a Maxwell element and a Kelvin-Voigt element and when are they useful?
- 12) Define resolved shear stress. Why is it important?
- 13) What is Schmid's law and the Schmid-factor?
- 14) What is meant by hardening and softening of a metal?
- 15) What is the critical plane approach?

## CHAPTER 7 Stress-life approach

### Not 7.5, 7.7, 7.8

- 1) How is a S-N-curve constructed?
- 2) Define fatigue limit. How is the fatigue limit defined if the S-N curve do not approach a constant value?
- 3) Which is the Basquin equation and when does it apply? Determine the number of cycles to fatigue as function of stress amplitude.
- 4) Define the diagram in which the Basquin equation is a straight line. What is the slope of the line?
- 5) The relation between stress amplitude  $\sigma_a$  and number of cycles to fatigue  $N$  is, for a specific material is in the interval  $100\text{MPa} < \sigma_a < 200\text{MPa}$  described by  $\sigma_a = -50 \log N + 400\text{MPa}$  assuming  $R=-1$ . Draw the Wöhler curve. Which amplitude can be allowed assuming a life of  $10^5$  cycles? (Answer 150MPa). If  $\sigma_a = 200\text{MPa}$ , determine the number of cycles to fatigue. (Answer  $10^4$  cykler).
- 6) Define  $R$ .
- 7) How is a mean stress  $\neq 0$ , i.e.  $R \neq -1$  compensated for? What are Soderberg, Gerber, Goodman and Haigh-diagrams?
- 8) Assume  $R = 0$ ,  $\sigma_e = 380\text{MPa}$  and  $\sigma_{TS} = 1200\text{MPa}$ . Determine maximum  $\sigma_a$  for infinite life. Compare Gerber and Goodman. (Answer: Gerber 348MPa, Goodman 289MPa.)
- 9) How did Morrow modify the Basquins equation?
- 10) What is the Palmgren-Miner rule? Which objections can be raised against?
- 11) Assume, according to Wöhler,  $\sigma_a = -55 \log N + 430\text{MPa}$  and  $\sigma_m = 0$ . A load sequence with amplitudes  $\sigma_a = 200, 180, 150$  and  $100\text{MPa}$  during  $N = 15, 20, 250$  and  $3000$ , respectively. Assume the Palmgren-Miner rule to apply. How many such load sequences can be applied? (Answer: 152).
- 12) How can residual stresses be enforced? Why is this useful? Compare example 7.6.1, Example problem: Effects of surface treatments.
- 13) Define  $K_t$ ,  $K_f$  and  $q$ . What are the implications of  $q=1$  and  $q=0$ ?
- 14) How is  $K_f$  used at HCF? Why is it applied to the stress range, only?
- 15) How is a multi axial stress state treated?
- 16) What is proportional and non- proportional loading?
- 17) How is the critical plane-approach applied at non-proportional loading?

## CHAPTER 8 Strain-life approach

### Not Example 8.1.3

1) A Ramberg-Osgood-material follows, assuming monotonic loading, the relation

$$\varepsilon = \frac{\sigma}{E} + \varepsilon_f \left( \frac{\sigma}{\sigma_f} \right)^{1/n}$$

Assume  $\sigma_f = 1227 \text{MPa}$ ,  $\varepsilon_f = 1.0$ ,  $E = 200000 \text{MPa}$ ,  $n = 0.13$ .

Draw the stress-strain diagram and mark  $\sigma_f$ ,  $\varepsilon_f$ ,  $E$ . What is the influence from  $n$ ?

2) A Ramberg-Osgood-material under cyclic loading is described by

$$\varepsilon = \frac{\sigma}{E} + \varepsilon'_f \left( \frac{\sigma}{\sigma'_f} \right)^{1/n'} = \frac{\sigma}{E} + \left( \frac{\sigma}{A'} \right)^{1/n'}$$

Assume  $\sigma'_f = 1355 \text{MPa}$ ,  $A' = \sigma'_f / (\varepsilon'_f)^{n'} = 1344 \text{MPa}$ ,  $E = 200000 \text{MPa}$ ,  $n' = 0.13$ . Draw the hysteresis loop if  $\sigma = \pm 600 \text{MPa}$ .

3) Assume load control. Draw the strain amplitude for a hardening/softening material?

4) Assume displacement control. Draw the stress amplitude for a hardening/softening material?

6) Which is the Coffin-Manson relation? When should it be applied?

7) Which is the Morrow relation? Draw, schematically, the elastic and plastic contributions to the total strain and define the limit between "long" and "short" life.

8) How is  $\sigma_m \neq 0$  compensated for?

9) Draw a  $(\log(2N), \log(\Delta\varepsilon/2))$ -diagram for Morrows relation if

$\sigma_m = 0$ ,  $\sigma_m = -100 \text{MPa}$ ,  $\sigma_m = 100 \text{MPa}$ . Determine  $(N_f)_i$  for each case and determine corresponding strain amplitudes. Assume for the steel SAE1045 that  $\sigma'_f = 1227 \text{MPa}$ ,  $\varepsilon'_f = 1.0$ ,  $E = 200000 \text{MPa}$ ,  $b = -0.095$ ,  $c = -0.66$ .

10) The Neuber rule reads:  $K_f = \sqrt{K_\sigma K_\varepsilon}$ . What is the rationale for this?

11) What is the Neuber hyperbola and how is it used?

12) A plate contains a small, centrally placed circular hole. The plate is loaded by the remote stress  $S = \sigma_\infty = \pm 400 \text{MPa}$ . Determine number of cycles to failure according to the Neuber method. Assume a Ramberg-Osgood material model and use Morrows relation. Material data:  $q = 1$ ,  $E = 200000 \text{MPa}$ ,  $A' = 1344 \text{MPa}$ ,  $n' = 0.18$ ,

$\sigma'_f = 1227 \text{MPa}$ ,  $\varepsilon'_f = 1.0$ ,  $b = -0.095$ ,  $c = -0.66$

(Answer: 600 cycles)

Draw the hysteresis loop for  $S = \sigma_\infty = \pm 400 \text{MPa}$ .

Draw the hysteresis loop for  $S = \sigma_\infty = 200 \pm 200 \text{MPa}$ .

Determine number of cycles to fatigue using the Neuber method if

$S = \sigma_\infty = 200 \pm 200 \text{MPa}$ .

13) The stress levels in a load sequence are (MPa) 1,8,3,11,1,5,3,8,6,10,3,8,1,11,2,7,6,7,6,7,6,10,1,8,3,11. Identify load cycles using rain flow count.

14) How can an effective strain be determined?

**CHAPTER 9 Fracture mechanics and its implications for fatigue  
Overview 9.3.2, 9.7.6. Not 9.5.3. Overview 9.9 – 9.11.**

- 1) What is the Griffith fracture theory.
- 2) Define the energy release rate  $G$ .
- 3) (Show that  $G = \frac{F^2}{2B} \frac{dC}{da}$  applies to load control as well to displacement control.)
- 4) The fracture criterion is  $G = G_c$ . What holds for  $dG/da$ ?
- 5) Define mode I, II and III. Which is most common?
- 6) By solving a boundary value problem the stress- and strain state in a crack tip vicinity can be determined. What singularity applies to the stress field? What about the strain field?
- 7) Define the stress intensity factors.
- 8) Why is, always,  $K_I \geq 0$ ?
- 9) In mode I the principal stresses are  

$$\sigma_1 = \frac{K_I}{\sqrt{2\pi r}} \cos \frac{\theta}{2} \left(1 + \sin \frac{\theta}{2}\right), \sigma_2 = \frac{K_I}{\sqrt{2\pi r}} \cos \frac{\theta}{2} \left(1 - \sin \frac{\theta}{2}\right), \sigma_3 = 0$$
at plane stress and  

$$\sigma_3 = 0.6 \frac{K_I}{\sqrt{2\pi r}} \cos \frac{\theta}{2}$$
in plane deformation. Draw the contour of  $\sigma_{effMises} = \text{constant}$  about the crack tip in plane stress and in plane strain.
- 10) What is the  $T$ -stress?
- 11) What is  $K$ -dominance?
- 12) What is the fracture toughness  $K_{Ic}$ ?
- 13) State the Paris law.
- 14) For an edge crack in a large plate  $K_I = 1.12\sigma_\infty \sqrt{\pi a}$ . A crack of initial length  $a = a_0$  is discovered as its length is  $a = 0.1a_c$ . Critical crack length is  $a_c$  where  $a_c/a_0 = 400$ . What portion of life remains as the crack is discovered? The exponent in Paris' law is  $n=3$ .
- 15) What is the relation between  $G$  and  $K$ ?
- 16) Solve Example 9.4.1 in Suresh.
- 17) The fracture criterion reads  $K_I = K_{Ic}$ . How do  $K_{Ic}$  vary with specimen width and temperature?
- 18) What is the  $J$ -integral measuring?
- 19) What is the relation between  $K - J - G$ ?
- 20) What is the HRR-singularity?
- 21) How is Crack Tip Opening Displacement, CTOD, defined? How can CTOD be used as a fracture criteria?
- 22) What is  $J$ -dominance?
- 23) Which is, according to ASTM, the limit for the use of LEFM? How is this limit defined?
- 24) Solve Example 9.7.5 in Suresh.
- 25) How is a hydrostatic stress state in the vicinity of a crack tip compensated for?

## **CHAPTER 13 Fretting fatigue**

**Overview. Focus on phenomena.**

- 1) Name some of the concepts of Table 13.1.
- 2) Illustrate the stick-slip-region as a sphere is pressed against a flat surface at the same time as cyclically varying shear forces are applied (Fig. 13.6).
- 3) Illustrate schematically the stress field emerging as a cylinder rolls over a flat surface (Fig. 13.7).
- 4) Name some different types of damage emerging due to fretting fatigue (Table 13.2).
- 5) What is a fretting map?